# (Dis)Solving the ZLB equilibrium through Income Policy<sup>\*</sup>

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#### Abstract

We investigate the possibility to reflate an economy experiencing a long-lasting ZLB episode with subdued or negative inflation, by imposing a minimum level of wage inflation. Our proposed income policy relies on the same mechanism behind past disinflationary policies, but it works in the opposite direction. It is formalized as a downward nominal wage rigidity (DNWR) such that wage inflation cannot be lower than a fraction of the inflation target. This policy allows to dissolve the ZLB steady state equilibrium in an OLG model featuring "secular stagnation" and in a infinite-life model, where this equilibrium emerges due to deflationary expectations.

*Keywords: Zero lower bound, Wage indexation, Income policy, Inflation expectations. JEL classification: E31, E52, E64.* 

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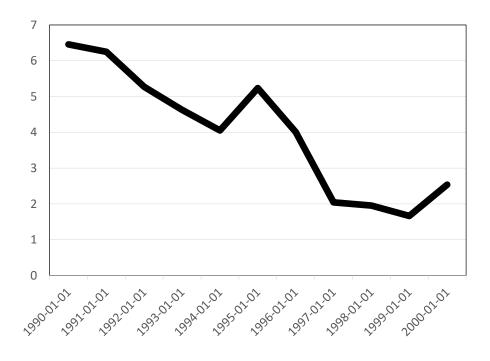
# **1** Introduction

Inflation rate in Italy was about 6% at the beginning of the '90s and it needed to decrease by about 4% in few years to satisfy the inflation Maastricht criterion. Figure 1 shows that Italy met the challenge. The Protocol signed by the employers and trade-union organizations on 23 July 1993 was the cornerstone for the structural reduction of inflation. It marked the definite dismantling of the automatic indexation to past inflation mechanism, and it established the price inflation expected (and targeted) by the government as a common reference for the indexation of national collective contracts.<sup>1</sup> The main channel that led to the successful disinflation was the realignment of inflation expectations to the target level chosen by government (Fabiani et al., 1998; Destefanis et al., 2005). The problem of Italy was a problem of "de-indexing" the economy by de-indexing the wage bargaining process and thus breaking the wage-price inflation spiral. This type of income policy was popular at the time, and many examples show that they could be a very efficient way to disinflate the economy.<sup>2</sup>

<sup>&</sup>lt;sup>1</sup>The 'Protocol on Incomes and Employment Policy, on Contractual Arrangements, on Labor Policies and on Support for the Production System' (*Protocollo sulla politica dei redditi e dell'occupazione, sugli assetti contrattuali, sulle politiche del lavoro e sul sostegno al sistema produttivo*) was drafted by the presidency of the Council of Ministers on 3 July 1993, under Prime Minister Carlo Azeglio Ciampi. The wage contracts indexation was based on the targeted inflation rate (*tasso d'inflazione programmata*) and not on actual or past inflation. While the automatic mechanism (the so-called *scala mobile*) had ceased to operate already in 1992, wage setting was still very much backward-looking.

<sup>&</sup>lt;sup>2</sup>In Australia, the Hawke government in March 1983 promoted Accord Mark I with the unions to restrain wage increases, in order to fight a period of high unemployment and high inflation. The Accord lasted 13 years and was renegotiated several times (Accords Mark I-VII). As a result of the improvement in industrial relations, a corporatist model emerged where the Australian Council of Trade Unions (ACTU) was regularly consulted over government decisions and was represented on economic policymaking bodies such as the board of the Reserve Bank of Australia. In the 1990s, the Dutch corporatist model (the so-called Polder model) gained popularity because of good social and economic performance. The Polder model is based on consulting between the government and the social partners, involving them in the design and implementation of socio-economic policies

Figure 1: Inflation rate (CPI, %) in Italy in the '90s. Source: FRED.



The Brazilian experience in the late 1990s is quite different from the Italian one, but it is another illustrative example of how de-indexing can be a powerful tool to coordinate inflation expectations and so to shift the economy from a high-inflation equilibrium to a low-inflation one. The Brazilian economy was plagued by extraordinary high inflation levels in the '80s, mainly caused by wage indexation.<sup>3</sup> In July

<sup>(</sup>see Visser and Hemerijck, 1997). Similar models are in place in Belgium and in Finland and other Scandinavian countries.

<sup>&</sup>lt;sup>3</sup> "Brazilian economists have long recognized that in a setting of full, compulsory indexation, orthodox monetary restraint is not a satisfactory answer to inflation. The idea that inflation has inertia, by virtue of the indexation law and practice, implies the need for an alternative stabilization strategy, namely, "heterodoxy." The issue is not only to control demand, but, more important, to coordinate a stop to wage and price increases, which feed on one another." (Dornbusch, 1997, p. 373)

1994, the so-called *Plano Real* was put in place in order to stabilize the economy. It introduced a new currency, i.e., Real Unity of Value (*Unidade Real de Valor or URV*), that was originally pegged 1:1 to the dollar. Initially, the new currency only served as unit of account, while the official currency, *cruzeiro*, was still used as mean of exchange. However, most contracts were denominated and indexed in the new currency, which was more stable than the *cruzeiro*. As a consequence, Brazilian consumers learned the possibility of price stability, inflationary expectations dropped and the inflationary spiral was arrested. The Plan succeeded for the psychological effect on inflation expectations and on the inflationary culture. Annual inflation decreased from 909.7% in 1994 to 14.8% in 1995 and then to 9.3% in 1996 and 4.3% in 1997.

What has all this to do with the zero lower bound (ZLB) problem and deflation or subdued inflation? The current macroeconomic scenario is starkly different: now, policy makers are not fighting against an inflationary spiral, rather central bankers are struggling to hit the inflation target and some advanced countries are still stuck in a liquidity trap, more than ten years after the global financial crisis. We argue that, although current problems are different from past ones, the solutions could be similar. Past disinflationary policies show that de-indexing the economy is an effective way to tackle inflation. The other side of the coin could be that "re-indexing" the economy is an effective way to tackle deflation. The idea is that all these plans were thought to stop the *upward* inertia in the behavior of inflation (or the so-called wage-price spiral). The problem in a ZLB (or in the path the lead to the ZLB) derives from the same logic, but it is a spiral *downward* rather than upward. This paper simply argues that policy should use the very same measures the other way round, that is, in the opposite direction.

This work puts forward a policy proposal able to avoid a "secular stagnation" and/or to eliminate a ZLB/deflationary equilibrium. We propose to simply impose a lower bound on wage inflation: an income policy based on a downward nominal wage rigidity (DNWR) such that wage inflation cannot be lower than a fraction of the intended inflation target. We show that with this simple DNWR constraint, it will always exists a level of inflation target that eradicates the ZLB equilibrium.

We show how our policy proposal works in two very different frameworks using the models in two influential papers in this literature: Eggertsson et al. (2019) (EMR, henceforth) and Schmitt-Grohé and Uribe (2017) (SGU henceforth). EMR is an overlapping generation (OLG) model of secular stagnation, where a ZLB equilibrium arises when the natural interest rate is negative. SGU is an infinite-life representative agent model, where a ZLB equilibrium can arise due to expectations of deflation, i.e., due to an expectation-driven liquidity trap à la Benhabib et al. (2001a,b). Both papers feature a DNWR constraint. We show that tweaking this constraint to allow for "reflationary income policy" eliminates the ZLB equilibrium, provided that the inflation target is sufficiently high. If wage inflation is sufficiently high, then there is no possibility for agents to coordinate on a deflationary or a secular stagnation equilibrium, because expectations of a deflation (or low inflation) and ZLB are not consistent with rational expectations. Our mechanism has the same flavour of the Italian case, but upside-down. Note that in equilibrium the DNWR does not bind, hence it is not the case that it is mechanically imposed. Moreover, both price and wage inflation are equal to the intended target and there is full employment in the unique equilibrium that survives. The DNWR acts as a coordination device that destroys the bad ZLB equilibrium.

EMR show that an increase in the inflation target in their model allows for a better outcome, but it cannot exclude a secular stagnation equilibrium. Hence they propose other possible demand-side solutions (especially fiscal policy). Our policy, instead, is a supply-side solution, as all the income policies. Our modification of the DNWR in those two models moves the aggregate supply curve, not aggregate demand. We believe this proposal to be a natural way of thinking about the ZLB problem. First, our approach recognizes the ZLB, and the often corresponding deflation or too low inflation problem, as a "nominal" problem. Second, once one sees the problem in this way, it is natural to think about it as a "reflation" problem, that is just the opposite of a disinflation. Many successful disinflationary policies in the '80s and '90s de-indexed the economy, using a set of policies (mainly income policies and some degree of corporatism) to engineer a reduction of inflation. Our proposal is just to adopt the same set of policies with the opposite goal: to re-index the economy in order to engineer a reflation.

Finally, note that we naturally chose two influential ZLB frameworks with a DNWR to present our analysis, given that we impose a DNWR. However, the DNWR is not a primitive feature of the economy, but rather we propose to use it as a policy instrument. Hence, our solution would work also if the economy is trapped in a ZLB/deflationary equilibrium without a binding DNWR to start with, and, hence, it does not feature unemployment in this equilibrium.

This paper is linked to an enormous literature on ZLB.<sup>4</sup> Two papers are how-

<sup>&</sup>lt;sup>4</sup>This literature focuses mostly in dynamics, studying the cost of the ZLB as a constrain to monetary policy (e.g., Gust et al., 2017), the effects of different monetary and fiscal policies around different equilibria (i.e., depending if the liquidity trap is fundamental or expectation-driven, e.g., Mertens and Ravn, 2014, Bilbiie, 2018) and on how to coordinate expectations to escape the liquidity trap

ever somewhat related to ours. Glover (2018) studies how a minimum wage policy affects the dynamic response of an heterogeneous agent model when the economy is hit by a persistent, but temporary, shock that drives the economy to the ZLB. Cuba-Borda and Singh (2019) consider a unified framework that simultaneously accommodates the secular stagnation hypothesis and expectation driven deflationary liquidity trap by assuming a preference for risk-free bonds in the utility function. Their paper focuses on quantitatively investigate the dynamic response of the economy to alternative policies around different steady states and to estimate the model on Japanese data. Their main result is that the estimates suggest that the expectation-driven liquidity trap à la Benhabib et al. (2001b) fits the Japanese data better. Moreover, the model incorporates the same DNWR constraint as in SGU. They show that this type of DNWR can eliminate the expectations trap equilibrium in SGU, but cannot eliminate the secular stagnation one. Our paper is very different in that it conceives the DNWR as a policy tool and not as a primitive. As such, we modify the DNWR and we link it to the inflation target. We show that such a specification could eliminate both the expectations trap equilibrium in SGU and the secular stagnation one in EMR. Hence, the policy is robust to the type of liquidity trap. Moreover, in their paper, as in EMR and SGU, increasing the inflation target cannot eliminate any of the two bad equilibria. In our framework, instead, it does and thus there is no issue of credibility of target due to the co-existence of multiple steady states. Furthermore, historical examples of past disinflationary policies suggest how to implement our policy proposal. Finally our approach is completely analytical, while their is numerical.

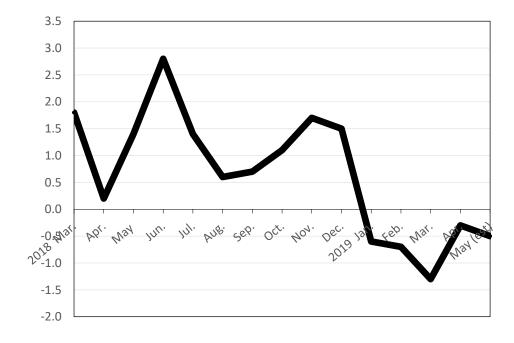
<sup>(</sup>e.g., Benhabib et al., 2002).

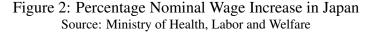
### **Policy relevance: the case of Japan**

The policy proposal is utmost relevant for Japan today, because it is tailored for an economy experiencing a long-lasting ZLB episode, which has not come to an end despite huge and prolonged monetary and fiscal interventions. The prime minister of Japan, Shinzo Abe, has long sought to influence wage negotiations to push for increases in nominal wages coherent with the inflation target. The wage negotiations between the Japan Business Federation (Keidanren) and the Trade Union Confederation (*Rengo*) occur during the "spring offensive" called *Shunto*, which is very influential because it sets the context for bargaining between individual companies and unions. However, in contrast with the Italian experience of consultation (i.e., *Concertazione*), the government does not take part in the negotiations, so the outcome fell well short of Mr. Abe's call for a 3% increase. Average wages (i.e., total cash earnings) increased by 0.1% in 2015, 0.6% in 2016 and 0.4% in 2017 according to data from the Japanese Ministry of Health, Labor and Welfare. Figure 2 shows the behavior from 2018 onward of average nominal wage increases (month-to-month in the preceding year). While the bargaining in 2018 was promising, average nominal wage growth turned *negative* in every month of 2019, hitting in March the lowest level of -1.3%.<sup>5</sup>

Dismal wage increases, despite a tight labor market, have thus become the biggest drag on the Japan efforts to reflate the economy. Our paper provides the theoretical underpinning in support of income policy to solve this problem. The goal of the income policy is to move all nominal variables in line with the BoJ's inflation

<sup>&</sup>lt;sup>5</sup>See e.g., "Shinzo Abes campaign to raise Japanese wages loses steam", FT online, 22 January 2019.





target. While a detailed discussion of policy implementation is outside the scope of the present paper, this is a crucial point that we now briefly discuss. First, as said, history provides many examples of successful implementation of income policy through some degree of corporatism to engineer a reduction of inflation. Hence, in some sense, this has already been done "the other way round". While the Italian institutional framework (i.e., *Concertazione*) or, more generally, moral suasion might not be a viable option for Japan, there could be other options available for the government to enforce wage inflation as, for example, the use of profit tax levy or subsidies (Wallich and Weintraub, 1971; Okun, 1978). From a policy perspective,

the IMF paper by Arbatli et al. (2016) is very related to ours. As we do, it advocates income policy as a possible "fourth arrow" to be added to Mr. Abe economic policy strategy to reflate the Japanese economy.<sup>6</sup> They discuss alternative policy options (on top of moral suasion) as a wage policy in the public sector and a "comply or explain" policy for firms in the private sector. The wage inflation target would not be a binding law, to allow movements in relative prices across the economy given differences in productivity and to take care of firms' competitiveness in domestic and international markets. The possible adverse impact on profitability, and possibly employment, in the short term could be a serious concern. In this sense, from a political economy perspective, a proposal of this type might have more support from unions than capitalists, so its political viability might depend on the relative power between these groups.

Moreover, according to commentaries and statements from government officials, the idea of a lack in consumption demand is behind the call for the wage increase. However, we argue this is the wrong way of looking at the problem: our solution is a supply side one. Expectations are such that the economy is trapped in a low inflation equilibrium, and a DNWR based on a minimal wage inflation is the supply side cure. A once-for-all increase in the level (vs. the rate of growth) of the minimum wage or of the consumption tax, as recently proposed by the government,<sup>7</sup> would not work. The cure is about engineering a reflation through a national

<sup>&</sup>lt;sup>6</sup>The paper has a completely different technical approach from ours. It simulates the Flexible System of Global Models (FSGM) developed by the Research Department of the IMF to analyze country-specific policy simulations in a global context. The simulations are based on a comprehensive set of monetary, fiscal and structural policies to mimic the "three arrows" policy of the Japanese government. On top of this, the authors add income policy, which is fed into the model as shocks to expectations of both price and wage inflation.

<sup>&</sup>lt;sup>7</sup>See, e.g., "Labor ministry panel suggests hiking minimum wage by  $\pm 27$  to push Japan average above  $\pm 900$ ", The Japan Times online, 31 July 2019. The consumption tax was already raised from

agreement (as in the Italian experience) between employers and union associations and the government to determine a sustained wage inflation, and about changing the deflationary psychology (as for the Brazilian Real Plan); it is not about a wage or price level increase.

The paper proceeds as follows. Section 2 presents how our policy would work in the EMR model, while Section 3 does the same in the SGU model. Section 4 concludes.

# 2 Reflation in the EMR OLG model

In sections 2.1 and 2.2, we carefully spell out the EMR model. Once the reader has grasped the logic of the equilibria in the EMR model, then it would be straightforward to understand our main result and the implications of our policy proposal in section 2.3.

## 2.1 The EMR OLG model

EMR study an economy with overlapping generations of agents who live three periods, firms and a central bank in charge of monetary policy (Appendix A.1 spells out the details and the derivations of the model). Population grows at a rate  $g_t$  and there is no capital in the economy.

Young households borrow up to an exogenous debt limit  $D_t$  by selling a oneperiod riskless bond to middle-aged households, which supply inelastically their

<sup>5%</sup> to 8% in April 2014. Now, the Japanese government plans to raise it to 10%. See, e.g., "Abe sticks with plan to raise Japan's consumption tax despite weak tankan results", The Japan Times online, 1 July 2019.

labor endowment  $\overline{L}$  for a wage  $W_t$  and get the profits  $Z_t$  from running a firm. Only middle-aged households work and run a firm. Generations exchange financial assets in the loan market, and in equilibrium the total amount of funds demanded by young households equals the one supplied by middle-aged ones. Old agents simply dissave and consume their remaining wealth. As in any OLG model, the equilibrium real interest rate,  $r_t$ , is endogenously determined and clears the asset market. It coincides with the natural interest rate, i.e.,  $r^f$ , when output is at potential, i.e.,  $Y^f$ .

The production technology of firms exhibits decreasing returns to labor,  $L_t$ , which is the only input of production. The labor market operates under perfect competition. However, workers are unwilling to supply labor for a nominal wage lower than a minimum level, so that

$$W_t = \max\left\{W_t^*, \alpha P_t \bar{L}^{\alpha - 1}\right\},\tag{1}$$

where  $W_t^*$  is the lower bound on the nominal wage,  $\alpha$  measures the degree of decreasing returns to labor and  $P_t$  is the price level. The DNWR is key in the model to generate a ZLB equilibrium. As in Schmitt-Grohé and Uribe (2016), we make the simple assumption that the minimum level is proportional to the nominal wage in the previous period:

$$W_t^* = \delta W_{t-1},\tag{2}$$

where  $\delta \leq 1.^{8}$  The labor market does not necessarily clear because of downwardly

<sup>&</sup>lt;sup>8</sup>This assumption is consistent with the empirical evidence in Schmitt-Grohé and Uribe (2016). A more general specification would allow the DNWR to depend on the level of employment or unemployment as in EMR and SGU, respectively. Our results will be unaffected by this alternative assumption. Hence, without loss of generality, we prefer to start with the simplest case for better intuition. EMR assume  $W_t^* = \gamma W_{t-1} + (1 - \gamma) \alpha P_t \bar{L}^{\alpha - 1}$ , such that the minimum nominal wage is the weighted average of the past wage level and the "flexible" level corresponding to full employment,

rigid wages. If labor market clearing requires a wage  $W_t$  larger than  $\delta W_{t-1}$ , the DNWR constraint is not binding, thus the nominal wage is flexible and the aggregate labor demand equals the economy's labor endowment, i.e.,  $L_t = \bar{L}$ . On the contrary, if labor supply exceeds labor demand at the wage  $W_t = \delta W_{t-1}$ , the wage cannot decrease further because of the DNWR constraint, so that involuntary unemployment arises, i.e.,  $L_t < \bar{L}$ .

The model is closed with a standard Taylor rule that responds only to inflation and it is subject to the ZLB constraint, that is

$$1 + i_t = \max\left[1, \left(1 + r_t^f\right)\Pi^*\left(\frac{\Pi_t}{\Pi^*}\right)^{\phi_{\pi}}\right],\tag{3}$$

where  $\phi_{\pi} > 1$ .  $\Pi_t = \frac{P_t}{P_{t-1}}$  is the gross inflation rate at time *t*.  $\Pi^*$  is the gross inflation target, and  $r_t^f$  is the natural real interest rate, that is, the unique level of real interest rate compatible with full employment in the OLG model.

### 2.2 Steady State Equilibrium in the EMR OLG model

Figure 3 conveniently shows the steady state relationships implied by this model, using an aggregate demand (AD) and aggregate supply (AS) diagram (see A.1 for the derivation). Both curves are characterized by two regimes and thus they both exhibit a kink.

Whether or not the DNWR constraint, (1), is binding defines the two regimes in the AS curve. The AS curve is vertical at the full employment level,  $Y^f = \bar{L}^{\alpha}$ , when  $\overline{i.e., \alpha P_t \bar{L}^{\alpha-1}}$ . We present this case in Appendix A.2. Moreover, we will present the somewhat similar case in which the minimum wage depends on unemployment as in SGU in the next section.

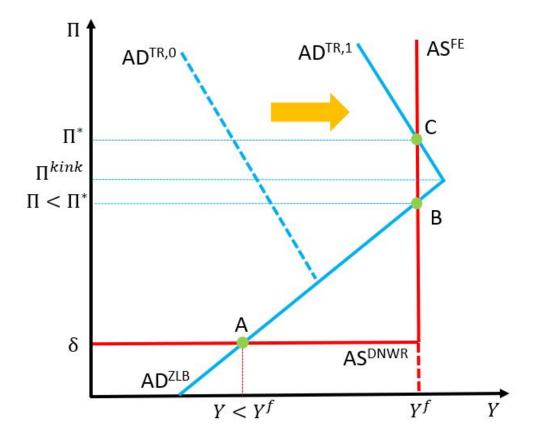


Figure 3: Aggregate demand and supply curves in the EMR model

(1) is not binding and  $W = \alpha P \bar{L}^{\alpha-1}$ .<sup>9</sup> Otherwise,  $W_t = W_t^* = \delta W_{t-1} \ge \alpha P_t \bar{L}^{\alpha-1}$ . This is a situation in which steady state wage and price inflation are equal to  $\delta$ , while the level of the real wage is  $\frac{W_t}{P_t} \ge \alpha \bar{L}^{\alpha-1}$ . The *AS* is thus flat at  $\Pi^W = \Pi = \delta$  for  $\forall L \le \bar{L}$ , and the level of employment (and output) is demand determined along the *AS*<sup>DNWR</sup>.

Whether or not the ZLB constraint, (3), is binding defines the two regimes for the *AD* curve. When the ZLB is not binding and monetary policy follows the Taylor

<sup>&</sup>lt;sup>9</sup>Note that we can suppress the time subscripts t, because we are just considering steady state relationships, where variables are constant.

rule, the AD curve in steady state is given by

$$Y_{AD}^{TR} = D + \left(\frac{1+\beta}{\beta}\right) \left(\frac{1+g}{1+r^f}\right) \left(\frac{\Pi^*}{\Pi}\right)^{\phi_{\pi}-1} D,\tag{4}$$

where  $\beta$  is the subjective discount factor. Assuming the Taylor principle is satisfied (i.e.,  $\phi_{\pi} > 1$ ), equation (4) defines a negative relationship between steady state inflation and output. When the inflation rate is higher than the target, the nominal interest rate increases more than inflation, resulting in a higher real interest rate  $(r > r^f \text{ for } \Pi > \Pi^* \text{ in (3)})$  that increases savings and contracts demand. However, when the ZLB is binding, the steady state *AD* becomes

$$Y_{AD}^{ZLB} = D + \left(\frac{1+\beta}{\beta}\right)(1+g)\Pi D,$$
(5)

which defines a positive relationship between steady state inflation and output. The higher is inflation, the lower the real interest rate in this case, because the nominal interest rate is stuck at zero, and  $1 + r = 1/\Pi$ . We denote  $\Pi^{kink}$  the inflation rate at which (4) and (5) crosses, that is

$$\Pi^{kink} = \left[\frac{1}{(1+r^f)}\right]^{\frac{1}{\phi_{\pi}}} \Pi^* \frac{\phi_{\pi}-1}{\phi_{\pi}}.$$
(6)

 $\Pi^{kink}$  determines when the ZLB becomes binding.

To prepare ground for the intuition of our main result, Figure 3 depicts how the *AD* curve moves with the inflation target. An increase in the inflation target shifts out the downward sloping  $AD^{TR}$  part of the *AD* curve (and increases the absolute value of its negative slope), but it does not affect the upward sloping  $AD^{ZLB}$  part, as

evident from equations (4) and (5).<sup>10</sup> As a result, a higher inflation target shifts out the kink in the *AD*, hence  $\Pi^{kink}$  is an increasing function of  $\Pi^*$ .

The crossing between the AS and the AD curves identifies a steady state. A "secular stagnation" equilibrium arises when  $r^f < 0$ , as Figure 3 shows. For a negative natural interest rate, there can be two different cases (leaving aside a limit, non-generic case), depending on the level of the inflation target. In the first case (see the dashed line  $AD^{TR,0}$ ,  $AD^{TR}$  does not cross  $AS^{FE}$  so that there is a unique steady state at point A, given by the intersection between  $AD^{ZLB}$  and  $AS^{DNWR}$ . Hence, this is a demand-determined and stagnant steady state (secular stagnation), where  $i = 0, \Pi^W = \Pi = \delta$  and  $Y < Y^f$ . In the second case (see the solid line  $AD^{TR,1}$ ), there are three different steady states: (A) the ZLB-U equilibrium just described that features ZLB, steady state inflation lower than the target and unemployment:  $i = 0, \Pi = \delta < \Pi^*, Y \le Y^f$ ; (B) a ZLB-FE equilibrium that occurs at the intersection of the  $AD^{ZLB}$  and the  $AS^{FE}$ , and it features ZLB, steady state inflation lower than the target and full employment:  $i = 0, \Pi = \frac{1}{1+r^{f}} \leq \Pi^{*}, Y = Y^{f}; \Pi^{1}$  (C) a *TR-FE* equilibrium that occurs at the intersection of the  $AD^{TR}$  and the  $AS^{FE}$ , and it features a positive nominal interest rate, steady state inflation equal to the target and full employment:  $i > 0, \Pi = \Pi^*, Y = Y^f$ .

EMR study these equilibria.<sup>12</sup> Moreover, they consider which type of poli-

<sup>&</sup>lt;sup>10</sup>Figure 3 follows Figure 6 Panel A in EMR and the discussion therein in Section VI, p. 25. As EMR, we depict  $AD^{TR}$  as linear in Figure 3 for clarity, despite it being non-linear (the curve has an asymptote at Y = D). We will do the same for  $AD^{TR}$  in the SGU model. None of the results obviously depends on this.

<sup>&</sup>lt;sup>11</sup>As mentioned by EMR, this equilibrium is similar to the deflationary steady state analyzed in Benhabib et al. (2001b).

<sup>&</sup>lt;sup>12</sup>They show that the equilibria *ZLB-U* and *TR-FE* are determinate, while the equilibrium *ZLB-FE* is indeterminate. While they show it for their DNWR specification (see footnote 8), these results still hold in the simpler specification of this Section. Results are available upon request.

cies could avoid the secular stagnation steady state ZLB-U, which always exists for  $r^f < 0$ . The only possibility to eradicate this equilibrium is through policies that make the natural interest positive. An increase of public debt could do that, because it absorbs the extra savings that drag the equilibrium real interest rate down, eventually restoring a positive  $r^f$ . However, in their quantitative exercise, EMR shows that starting from a value of  $r^f = -1.47\%$  and a debt-to-GDP ratio of 118%, the debt-to-GDP ratio needs to almost double to 215% to reach a value  $r^f$  of 1% and then to cancel the secular stagnation equilibrium. Hence, while a minimum level of debt which eliminates this equilibrium always exists, this value might be very high and not necessarily sustainable and/or achievable.<sup>13</sup> EMR looks at alternative options to raise  $r^f$  to positive values, because in their model monetary policy is powerless. As explained earlier, an increase in the inflation target moves  $AD^{TR}$ , but move neither the  $AD^{ZLB}$  nor the AS. Hence, if the natural real interest rate is negative, a ZLB-U always exists no matter what the inflation target is.

In the next section we present our proposal such that an appropriate choice of the inflation target is always able to dissolve the secular stagnation equilibrium.

### **2.3** Dissolving the ZLB Equilibrium

We now present a policy proposal able to avoid a secular stagnation even if  $r^f < 0$ . As explained in the Introduction, the secular stagnation equilibrium ZLB-U van-

<sup>&</sup>lt;sup>13</sup>For example, Japan has been in a liquidity trap for about two decades, despite a debt-to-DGP ratio above 200%. In EMR words (p.41): "Such a large level of debt raises questions about the feasibility of this policy, for we have not modeled any costs or limits on the governments ability to issue risk-free debt-an assumption that may be strained at such high levels. While these results suggest that several reforms would tend to increase the natural rate of interest, the menu of options does not paint a particularly rosy picture relative to the alternative of raising the inflation target of the central bank."

ishes with our policy proposal. We demonstrate our proposal by a simple modification of equation (2) that defines the minimum level of wages  $W_t^*$  in the DNWR constraint (1) to

$$W_t^* = \delta \Pi^* W_{t-1}. \tag{7}$$

From an economic point of view, (7) implies that wage inflation cannot be lower than a certain fraction  $\delta$  of the inflation target,  $\Pi^*$ . Hence,  $\delta$  could be thought as the minimum degree of indexation of the wage growth rate to the inflation target. (7) captures the idea behind the disinflationary policies in Italy. Wage inflation is anchored to a target inflation rate,  $\Pi^*$ . However, while there the goal was to put a *ceiling* on the pressure for wage increases to *decrease* the rate of inflation, here the goal is to put a *floor* on wage deflation to *increase* the rate of inflation.

From an analytical point of view, comparing Figure 4 with Figure 3 reveals how this simple modification changes the results in the previous section. The main point is that (7) makes the AS curve to shift with the inflation target, because the  $AS^{DNWR}$ curve is now equal to  $\delta\Pi^*$ , rather than simply  $\delta$ , as in the EMR case. Hence, an increase in the inflation target shifts the  $AS^{DNWR}$  curve upward. As the AD curve is unchanged with respect to the previous section, raising the inflation target shifts out  $AD^{TR}$ , as in Figure 3. We are now in the position to state our main result in the following proposition.

**Proposition 1.** Assume  $r^f < 0$  and  $\delta < 1$ . Then, if  $\Pi^* > \frac{1}{\delta(1+r^f)}$ , there exists a unique, locally determinate, TR - FE equilibrium, where the ZLB is not binding, the inflation rate is equal to the target and output is at full employment, i.e., i > 0,  $\Pi = \Pi^*$ ,  $Y = Y^f$ .

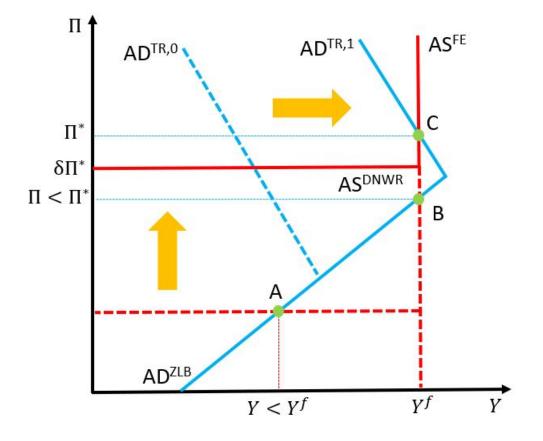


Figure 4: Raising the inflation target in the EMR model with our DNWR

In other words, it always exists a sufficiently high level of the inflation target,  $\Pi^*$ , such that the unique and locally determinate equilibrium features full employment and inflation at the target without binding ZLB. While the formal proof of Proposition 1 is in the Appendix A.1.3, Figure 5 displays the intuition very clearly. It shows five different panels, each for different ranges of values of the inflation target. As the inflation target increases, the economy moves from Panel A to Panel E. The key thing to note is that while the *AD* curve moves as described in the previous section, now also the *AS*<sup>DNWR</sup> shifts upward. For sufficiently high inflation target, the economy reaches the situation in Panel E, where only the *TR* – *FE* equi-

librium exists. Therefore, the secular stagnation equilibrium, ZLB - U, disappears if  $\Pi^* \ge \left[\delta(1+r^f)\right]^{-1}$ .

Let's turn to define the different equilibria in the Figure. As the level of the inflation target increases, five different cases (two of which are non generic) emerge: Panel A: if  $\Pi^* < 1/(1+r^f)$ , only the ZLB - U equilibrium exists at point A; Panel B: if  $\Pi^* = \frac{1}{1+r^f}$ , two equilibria exist: a ZLB - U equilibrium at point A and an equilibrium at point B/C that is a combination between ZLB - FE and TR - FE, where output is at full employment, the nominal interest rate prescribed by the Taylor rule is exactly zero and the inflation rate is equal to the target; Panel C: if  $\frac{1}{1+r^f} < \Pi^* < \frac{1}{\delta(1+r^f)}$ , three equilibria exist: ZLB - U at point A, ZLB - FE at point B and TR - FE at point C; Panel D: if  $\Pi^* = \frac{1}{\delta(1+r^f)}$ , two equilibria exist: TR - FE at point C and an equilibrium at point A/B that is a combination between ZLB - U and ZLB - FE, where output is at full employment, the ZLB is binding (and *i* is off the Taylor rule) and the inflation rate is lower than the target,  $\Pi = \delta\Pi^* < \Pi^*$ ; Panel E: if  $\Pi^* > \frac{1}{\delta(1+r^f)}$ , only the TR - FE equilibrium exists at point C.

Contrary to EMR where monetary policy is powerless, now monetary policy can wipe out the ZLB equilibrium by choosing an adequate inflation target. Alternatively, for a given  $r^f$ , one could choose  $\delta$  to reach a particular inflation target. Hence, interpreting our proposed solution in (7) as an income policy, for given values of  $r^f$  and of the intended inflation target, the condition  $\delta > [\Pi^*(1+r^f)]^{-1}$ gives the necessary value of  $\delta$  that determines the degree of indexation of nominal wages to the inflation target. Using the number in EMR, if  $r^f = -1.47\%$ , then  $\delta$  should be greater than 0.995 or 0.976 to reach an inflation target of 2% or 4%, respectively.

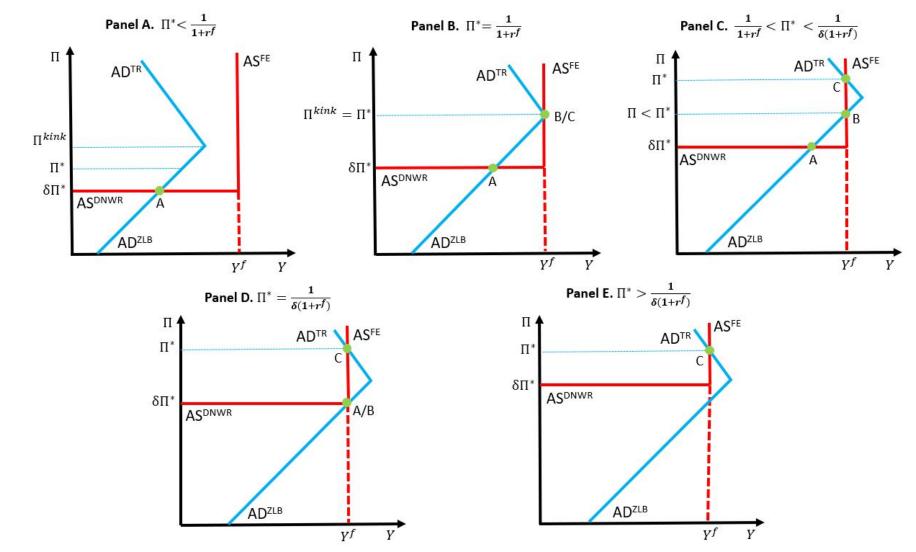


Figure 5: All possible steady state equilibria in the EMR model with our DNWR

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Finally, there is another important implication of our proposed policy with respect to EMR, that we summarize in the next proposition.

**Proposition 2.** Assume  $r^f < 0$  and  $\delta < 1$  and that the economy is trapped in a secular stagnation equilibrium, ZLB - U (Panel A). Then, an increase in the inflation target is always beneficial, in the sense that steady state output and inflation increase, irrespective if this increase is sufficient or not to escape the secular stagnation.

Any, however small, increase in the target shifts upwards the  $AS^{DNWR}$ , and thus it moves the secular stagnation equilibrium along the  $AD^{ZLB}$  increasing the level of output and inflation. This is depicted in Figure 5, where the ZLB - U equilibrium A in Panel A moves up in Panels B, C and D. This does not happen in the EMR specification. In Figure 3 both  $AD^{ZLB}$  and  $AS^{DNWR}$  curve do not change with the inflation target. As a result, a mild increase in the target does not affect the secular stagnation equilibrium ZLB - U at point A, capturing Krugman's (2014) idea of "timidity trap". Only sufficiently large changes in the target make the TR - FE equilibrium to appear.<sup>14</sup> Our model has a similar flavour, but has a quite different implication: while it is still true that the policy is subject to a "timidity trap" to escape the secular stagnation, in the sense that the inflation target should be sufficiently high to avoid it, an increase in the target is always beneficial.

<sup>&</sup>lt;sup>14</sup> "Small changes in the inflation target have no effect, capturing Krugman's observation of the "law of the excluded middle" or "timidity trap" when trying to explain why the Japanese economy might not respond to a higher inflation target announced by the Bank of Japan unless it was sufficiently aggressive." (EMR, p.3).

# **3** Reflation in the SGU infinite-life model

We now turn to a different model and to a different DNWR specification to show that our proposed policy works as well in this framework. The logic is very similar in this case, so, we still convey it mostly by using figures and put most of the derivations in Appendix A.3.<sup>15</sup>

## 3.1 Steady State Equilibrium in the SGU infinite-life model

SGU employs a simple flexible-price, infinite-life representative agent model to study the dynamics leading to a liquidity trap and a jobless recovery. With respect to the model in the previous section, they also employ a different specification of the DNWR constraint

$$\frac{W_t}{W_{t-1}} \ge \gamma(u_t) = \gamma_0 \left(1 - u_t\right)^{\gamma_1} = \gamma_0 \left(\frac{L_t}{\bar{L}}\right)^{\gamma_1}.$$
(8)

The DNWR implies that the lower bound on wage inflation depends on the level of unemployment, u, or on the employment ratio  $L/\overline{L}$ . When L = 0 (or u = 1) the lower bound is zero, then it increases with employment with elasticity  $\gamma_1$ , and at full employment wage inflation cannot be lower than  $\gamma_0$ . SGU imposes the following important assumption on  $\gamma_0$ :  $\beta < \gamma_0 \le \Pi^*$ , where  $\beta$  is the subjective discount factor of the representative agent. For simplicity, we assume  $\gamma_0 = \Pi^*$ , as SGU do in their quantitative calibration. The DNWR (8) implies the following complementary

<sup>&</sup>lt;sup>15</sup> Compared to the original model in SGU, we abstract from growth, from the shocks and from fiscal policy. Our results are unaffected by this modification.

slackness condition

$$(\bar{L} - L_t) \left[ W_t - \gamma_0 \left( 1 - u_t \right)^{\gamma_1} W_{t-1} \right] = 0$$
(9)

that ties down quite strictly the type of equilibrium under unemployment. If  $L_t < \overline{L}$ , then in steady state it follows  $W_t/W_{t-1} \equiv \Pi^W = \Pi = \gamma_0 (1 - u_t)^{\gamma_1} < \gamma_0 = \Pi^*$ . Hence, steady state inflation is below the target whenever there is positive unemployment.

Similar to the previous model, thus there are two regimes characterizing the AS in steady state. First, AS is vertical at full employment:  $Y_{AS}^{FE} = Y^f = \bar{L}^{\alpha}$ . Second, the  $AS^{DNWR}$  is upward sloping in the presence of unemployment due to the binding DNWR constraint:

$$Y_{AS}^{DNWR} = \left[ \left( \frac{\Pi}{\gamma_0} \right)^{\frac{1}{\gamma_1}} \bar{L} \right]^{\alpha}.$$
 (10)

The two branches of the *AS* meet at the kink when  $\Pi_{AS}^{kink} = \gamma_0$ , hence, at the inflation target under our simplifying assumption  $\gamma_0 = \Pi^*$ .

The demand side is shaped by a monetary policy rule with a ZLB

$$1 + i_t = \max\left\{1, 1 + i^* + \alpha_\pi \left(\Pi_t - \Pi^*\right) + \alpha_y \ln\left(\frac{Y_t}{Y^f}\right)\right\}$$
(11)

where  $1 + i^* = \Pi^* / \beta$ . In steady state (11) becomes

$$\ln Y_{AD}^{TR} = \ln Y^f - \frac{\beta \alpha_{\pi} - 1}{\beta \alpha_y} \left( \Pi - \Pi^* \right)$$
(12)

for 1 + i > 1. This equation yields a negative steady state relationship between output and inflation, if monetary policy is active ( $\beta \alpha_{\pi} > 1$ ), as in EMR model.

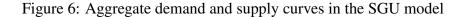
The main difference between an OLG model, as in EMR, and an infinite-life

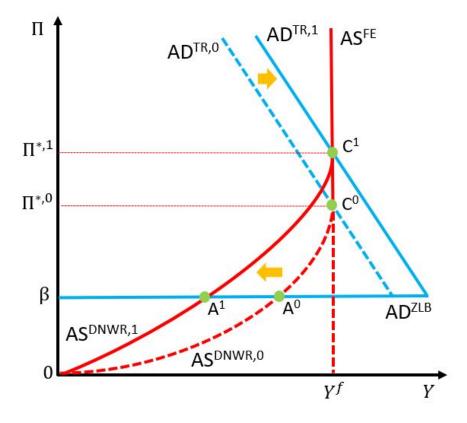
model, as in SGU, lies in the steady state determination of the equilibrium/natural real interest rate. Given the Euler equation, the inverse of the subjective discount factor  $\beta$  pins down the natural real interest rate in an infinite-life representative agent model, so the latter does not depend on the supply and demand of assets in the economy as in an OLG model. This has important implications for the shape of the AD, because the  $AD^{TR}$  is downward sloping as in the EMR model, but  $AD^{ZLB}$  is now horizontal in this model, rather than upward sloping. If the ZLB is binding, the steady state inflation rate must equal to  $\beta$ , because i = 0 and  $1 + r = 1/\beta$ , whatever the level of steady state output. AD is therefore flat at  $\Pi = \beta$ , and steady state output is determined by the AS.

Figure 6 shows the AS - AD diagram for the SGU model. The assumption in SGU  $\beta < \gamma_0 \leq \Pi^*$  guarantees that it does not exists an intersection between  $AS^{FE}$  and  $AD^{ZLB}$ . Moreover, there cannot be also an intersection between  $AD^{TR}$ and  $AS^{DNWR}$ .<sup>16</sup> Given these assumptions, there are always two equilibria.<sup>17</sup> As in the previous section, point  $A^0$  is a ZLB - U type of equilibrium, where both the ZLB and the DNWR constraints are binding, while point  $C^0$  is a TR - FE one, where none of the two constraints is binding, the economy is at full employment and inflation at target.<sup>18</sup> The Figure also shows what happens when the inflation

<sup>&</sup>lt;sup>16</sup>For any  $\Pi \leq \Pi^*$ ,  $Y_{AS}^{DNWR} \leq Y^f \leq Y_{AD}^{TR}$ , which goes through the point  $(Y^f, \Pi^*)$ . <sup>17</sup>There are no restrictions on  $\gamma_1$ . So we can distinguish three cases: if  $\gamma_1 > \alpha$ , the  $AS^{DNWR}$  is convex as depicted in Figure 6; it is concave for  $\gamma_1 < \alpha$ ; and it is a straight line when  $\gamma_1 = \alpha$ . Whether the AS<sup>DNWR</sup> is convex or concave (or a straight line) does not affect our results qualitatively, but the ZLB - U equilibrium  $A^0$  is associated with a larger negative output gap when  $AS^{DNWR}$  is concave (or a straight line).

<sup>&</sup>lt;sup>18</sup>Although point  $A^0$  in Figure 6 features  $Y < Y^f$ ,  $\Pi < \Pi^*$  and i = 0, it is not determinate, contrary to the corresponding equilibrium in the EMR OLG model. Rather, it is indeterminate as B in Figure 3. Furthermore, the ZLB - U equilibrium in the SGU model does not reflect the idea of secular stagnation as described in Summers (2015) that entails  $r^{f} < 0$ . Therefore, we define it *deflationary* equilibrium ( $\Pi = \beta < 1$ ), instead of *secular stagnation* one.





target increases:  $AD^{TR}$  shifts out, as before, but now  $AS^{DNWR}$  moves to the left. A higher target increases  $\gamma_0 = \Pi^*$ , hence makes the  $AS^{DNWR}$  steeper (see (10)). It follows that raising the inflation target is detrimental in this model for a liquidity trap equilibrium. As the steady state inflation is always equal to  $\beta$  on the  $AD^{ZLB}$ , an increase in the target enlarges the inflation gap,  $\Pi/\Pi^*$ , and the binding DNWR dictates higher unemployment in equilibrium.

### **3.2** Dissolving the ZLB equilibrium

We now adapt our policy proposal to this model. Recall that the idea is to reflate the economy by using the DNWR constraint to impose *a floor to the rate of growth of nominal wages that depends on the inflation target*. (8) does not do that because wage inflation is bounded by zero, when employment is zero. To see how our policy proposal would also work in this model, let's simply modify the DNWR (8) in a similar vein as (7)

$$\frac{W_t}{W_{t-1}} \ge \delta \Pi^* + \gamma(u_t) = \delta \Pi^* + \gamma_0 \left(1 - u_t\right)^{\gamma_1},\tag{13}$$

assuming now that  $\beta < \delta \Pi^* + \gamma_0 \le \Pi^*$ , which is the equivalent assumption to  $\beta < \gamma_0 \le \Pi^*$  in the SGU case. Accordingly the *AS*<sup>DNWR</sup> becomes

$$Y_{AS}^{DNWR} = \left[ \left( \frac{\Pi - \delta \Pi^*}{\gamma_0} \right)^{\frac{1}{\gamma_1}} \bar{L} \right]^{\alpha}.$$
 (14)

Figure 7 shows how this modification yields similar implications as in the previous case. Panel A displays the two equilibria, ZLB - U and TR - FE, with our modified DNWR. The other two panels show what happens when the inflation target increases. Panel B shows that a too timid increase in the target has perverse effects: unemployment goes up in the ZLB - U equilibrium, for the same level of deflation,  $\Pi = \beta$ . Krugman's (2014) timidity trap is *enhanced*: an increase in the target worsens the deflationary equilibrium. As explained above, this follows directly from the assumption on the DNWR constraint: a larger inflation gap calls for a higher unemployment. This is an important warning to remember regarding

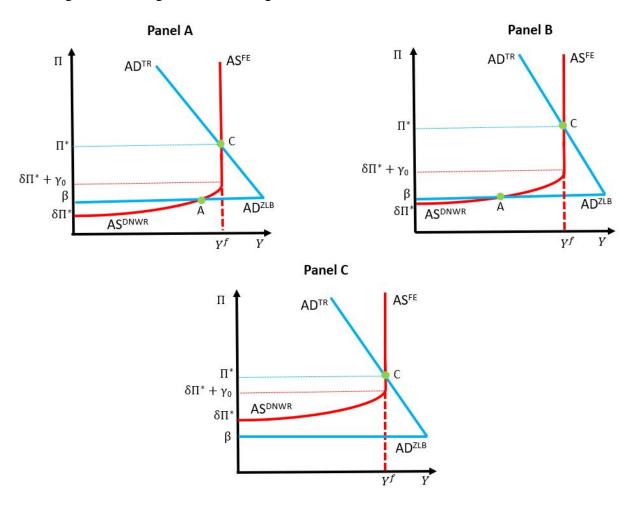


Figure 7: Raising the inflation target in the SGU model with our DNWR

the implementation of our policy proposal. If an increase in the target causes the indexation policy to force the wages to increase by more, but agents do not adjust their inflation expectations upwards, then a deflationary equilibrium still exists, but higher unemployment is needed to support it. This result is the opposite of Proposition 2 in section 2.3. However, this stark difference is not due to the different DNWR. Indeed, Appendix A.2 shows that Proposition 2 is robust to the case in which the DNWR constraint depends on employment (as in the original EMR's

work).

The crucial difference between these two models lies on the demand side, and more precisely, on  $AD^{ZLB}$ . The latter is upward sloping and steeper than the  $AS^{DNWR}$ in an OLG model, because an increase in steady state inflation decreases the real interest rate, spurring demand, when the ZLB is binding. In an infinite-life representative agent economy, instead, the real interest rate is not endogenously determined, but it is given by  $1/\beta$ . It follows that steady state inflation is given ( $\Pi = \beta$ ) in a ZLB equilibrium. This has two key implications. First, there is no positive effect on demand of an increase in the inflation target in a ZLB equilibrium. Second, price inflation is given, so inflation expectations do not adjust to the intended increase in wage inflation in the ZLB equilibrium. In other words, wage inflation has to be equal to price inflation, that is, equal to  $\beta$  in the ZLB equilibrium. Hence, any attempt to increase wage indexation by linking the increase in the nominal wages to a higher inflation target has to be compensated by higher unemployment, given the DNWR (13). The liquidity trap gets worse, because the policy is trying to force an increase in wage inflation, but agents don't believe prices could increase. Prices are actually decreasing in equilibrium. The increase in the inflation target is too timid, hence unless agents change their expectations by moving to the other TR - FEequilibrium, the ZLB equilibrium survives and actually worsen.

Panel C shows that for a sufficiently high inflation target, however, deflationary expectations cannot be supported in equilibrium. From an a analytical point of view, this happens for  $\Pi^* > \beta/\delta$ . Intuitively, by forcing the increase in wage inflation above a certain threshold, there is no level of unemployment that support the ZLB equilibrium. As the effect on inflation expectations of the Brazilian Real Plan induced the switch from one inflationary equilibrium to a stable inflation one, our DNWR constraint acts as a coordination device for agents on the now unique TR - FE equilibrium. It is reasonable to think that the switch might actually happen before reaching the limit of u = 1 as in this simple framework. At a certain point the level of unemployment would become unsustainable, so that agents would be compelled to coordinate on higher inflation expectations, that is, on the TR - FEequilibrium. We can rearrange the condition that guarantees a unique equilibrium of the type TR - FE as  $\delta > \beta/\Pi^*$ . This provides the degree of wage indexation necessary to achieve a specific inflation target, for a given discount factor. If  $\beta = 0.95$ , an inflation target of 2% (4%) requires  $\delta$  greater than 0.93 (0.91) to be sustained.<sup>19</sup>

We conclude by stating two propositions that parallel those in the previous section for the OLG model.

**Proposition 3.** Assume  $\beta < \delta \Pi^* + \gamma_0 \leq \Pi^*$ . Then, if  $\Pi^* > \beta/\delta$ , there exists a unique, locally determinate, TR - FE equilibrium, where the ZLB is not binding, the inflation rate is equal to the target and output is at full employment, i.e., i > 0,  $\Pi = \Pi^*$ ,  $Y = Y^f$ .

**Proposition 4.** Enhanced Timidity Trap. Assume  $\beta < \delta \Pi^* + \gamma_0 \leq \Pi^*$  and that the economy is trapped in a deflationary equilibrium, ZLB - U (Panel A). Then, an increase in the inflation target is always detrimental, in the sense that steady state output decreases in a ZLB equilibrium, unless this increase is sufficient to escape deflation.

<sup>&</sup>lt;sup>19</sup>If we assume a deterministic trend in productivity as in SGU, the necessary level of  $\delta$  to sustain any given inflation target declines.

# 4 Conclusions

We have presented here a policy proposal to reflate economies experiencing a longlasting ZLB episode with subdued or negative inflation. The ZLB problem is a "nominal" problem, in the sense that, for any level of the real interest rate, there is always a minimum inflation level that prevents a liquidity trap. As de-indexing the economy has been proved an effective way to tackle high inflation in past historical episodes, we suggest to apply the same mechanism, but in the opposite direction, to engineer inflation. More precisely, our policy of "re-indexing" the economy consists in imposing a minimum wage inflation that delivers the necessary price inflation to escape from the ZLB.

In order to prove the validity of our proposed income policy, we have studied the ZLB problem through the lens of the OLG model of EMR and the infinitelife representative agent model of SGU, which both feature a ZLB equilibrium and downwardly rigid nominal wages. Our proposal is to impose *a floor on wage inflation that depends on a fraction of the inflation target* through the downward nominal wage rigidity. This is exactly the opposite of the ceiling on wage inflation imposed in some past disinflationary policies. Under our assumption, the ZLB equilibrium disappears in both models. Note that in equilibrium the DNWR does not bind, hence it is not mechanically imposed. Moreover, both price and wage inflation are equal to the intended target and there is full employment in the unique equilibrium that survives. The DNWR acts as a coordination device that destroys the bad ZLB equilibrium. This result is robust to the specification of the downward nominal wage rigidity, and it requires a sufficiently high inflation target. Indeed, if the lower bound on wage inflation is not high enough, the economy is trapped in the Krugman's (2014) "timidity trap".

The timidity trap highlights the differences between the OLG and the infinitelife model, leading to different implications of our policy proposal according to the model. Raising the inflation target when nominal wage growth is indexed to it mitigates the ZLB problem in the OLG model, even if the increase is not sufficient to lift the economy out of the liquidity trap. Indeed, a higher target transmits to price inflation via wage indexation and this in turn reduces the real interest rate, stimulating demand and output. This novel result is overturned in an infinite-life model, because the equilibrium real interest rate is fixed and thus the inflation level is equal to discount factor in the ZLB equilibrium. The higher inflation target does not translate in higher price inflation, and, given the DNWR constraint, the ZLB equilibrium features even lower output because of a larger inflation gap.

Finally, three issues would deserve further investigation. First, our simplified models do not exhibit a transitional dynamics from the ZLB equilibrium to an equilibrium with full employment and inflation at the target, which would instead be entailed by more realistic models (for example, with capital). Although the transitional dynamics constitutes an interesting future direction of our research and the associated costs cannot be disregarded, we don't think this could really affect our results. Indeed, our policy proposal is thought for economies that are stuck in a ZLB equilibrium, where output is chronically lower than the potential and inflation never hits the targeted level. Japan is the most prominent example. In a such a scenario, it is very hard to think that the gains in terms of output and inflation of escaping from the ZLB could be lower than the cost associated with the transitional dynamics. Second, we abstract from the presence of shocks. However, a tight DNWR con-

straint would impede the short-run adjustment of the economy to shocks, especially supply shocks, requiring a flexible real wage. This lack of flexibility would obviously impose short-run costs to the economy. Third, the pass-through from wage to price inflation could be affected by international competition in an open economy context, if the goods market is not longer perfectly competitive but national and foreign firms supply different varieties of goods. Indeed, firms could only partially transmit the higher labor costs to prices to preserve their competitiveness. If the exchange rate is flexible, a devaluation of the national currency can compensate for the higher prices, preserving the market shares of firms in the international markets. Moreover, a depreciated currency can contribute to boost inflation via the higher cost of imported goods. On the contrary, in the case of a monetary union (or a currency area in general), coordination among the member states is necessary to implement our policy proposal. Otherwise, countries that implement our income policy would suffer an appreciation in real terms with respect to those that do not, with negative consequences in terms of current account imbalances.

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# A Appendix

# A.1 Appendix to EMR

### A.1.1 Model

The maximization problem of the representative household is

$$\max_{C_{t+1}^m, C_{t+2}^o} E_t \left\{ \ln C_t^y + \beta \ln C_{t+1}^m + \beta^2 \ln C_{t+2}^o \right\}$$

s.t.

$$C_t^y = B_t^y \tag{A1}$$

$$C_{t+1}^{m} = Y_{t+1} - (1+r_t)B_t^{y} - B_{t+1}^{m}$$
(A2)

$$C_{t+2}^o = (1 + r_{t+1}) B_{t+1}^m \tag{A3}$$

$$(1+r_t)B_t^y = D_t, (A4)$$

where  $Y_t = \frac{W_t}{P_t}L_t + \frac{Z_t}{P_t}$ .<sup>20</sup>  $C_t^y$ ,  $C_{t+1}^m$  and  $C_{t+2}^o$  denote the real consumption of the generations, while  $B_t^y$  and  $B_{t+1}^m$  are respectively the real value of bonds sold by young households and bought by middle-aged ones. Equation (A4) represents the debt limit, which is assumed to be binding for the young generation.<sup>21</sup> The optimality condition for the maximization problem is the standard Euler equation

$$\frac{1}{C_t^m} = \beta \, (1+r_t) E_t \frac{1}{C_{t+1}^o}.$$
 (A5)

Generations exchange financial assets in the loan market, whose equilibrium condition is

$$(1+g_t)B_t^y = B_t^m. (A6)$$

The loan demand on the left-hand side of (A6) can be denoted with  $L_t^d$  and alternatively expressed as

$$L_t^d = \left(\frac{1+g_t}{1+r_t}\right) D_t \tag{A7}$$

by using (A4) to substitute for  $B_t^y$ . Combining (A2), (A3), (A4) and (A5) yields the loan supply

$$L_t^s = \frac{\beta}{1+\beta} \left( Y_t - D_{t-1} \right). \tag{A8}$$

<sup>&</sup>lt;sup>20</sup> Labor demand  $L_t$  does not necessarily equate labor supply  $\bar{L}$ , as explained above.

<sup>&</sup>lt;sup>21</sup> This assumption holds for  $D_{t-1} < \frac{1}{1+(1+\beta)\beta}Y_t$ .

The market clearing real interest rate which equates (A7) and (A8) is

$$(1+r_t) = \frac{(1+g_t)(1+\beta)D_t}{\beta(Y_t - D_{t-1})}$$
(A9)

and it coincides with the natural interest rate

$$\left(1 + r_t^f\right) = \frac{(1 + g_t)(1 + \beta)D_t}{\beta \left(Y^f - D_{t-1}\right)}$$
(A10)

at the potential level of output  $Y^f$ .

Each middle-aged household runs a firm that is active for just one period in a perfectly competitive market. The production technology of firms is given by

$$Y_t = L_t^{\alpha} \tag{A11}$$

where  $0 < \alpha < 1$ . Profits are

$$Z_t = P_t Y_t - W_t L_t \tag{A12}$$

and they are maximized, under the technological constraint (A11), if the real price of labor equals its marginal productivity,

$$\frac{W_t}{P_t} = \alpha L_t^{\alpha - 1}.$$
(A13)

Wages are subject to the DNWR constraint (1) that we report again here

$$W_t = \max\left\{W_t^*, \alpha P_t \bar{L}^{\alpha - 1}\right\},\tag{A14}$$

where the lower bound on the nominal wage,  $W_t^*$ , is given by (2). Finally, the standard Fisher equation holds:

$$1 + r_t = (1 + i_t) E_t \Pi_{t+1}^{-1}, \tag{A15}$$

where  $E_t$  denotes the expectation operator.

#### A.1.2 Steady State Equilibrium

A competitive equilibrium is a set of quantities  $\{C_t^y, C_t^m, C_t^o, B_t^y, B_t^m, Y_t, Z_t, L_t\}$  and prices  $\{P_t, W_t, r_t, i_t\}$  that solve (1), (3), (A1), (A2), (A3), (A4), (A5), (A6), (A11), (A12), (A13) and (A15), given  $\{D_t, g_t\}$  and initial values for  $W_{-1}$  and  $B_{-1}^m$ . Here we study the steady state equilibrium, which can be represented by aggregate demand

and supply.

AS is characterized by two regimes, which depend on equation (1) through the steady state inflation rate. For  $\Pi \ge \delta$ , AS can be derived from equations (1), (A11) and (A13):

$$Y_{AS}^{FE} = \bar{L}^{\alpha} = Y^f.$$

Otherwise, the aggregate supply is given by

$$\Pi = \delta.$$

The regime of AD depends on the lower bound on the nominal interest rate expressed in equation (3). For a positive nominal interest rate (1 + i > 1), we get the following AD by combining equations (3), (A9) and (A15):

$$Y_{AD}^{TR} = D + \left(rac{1+eta}{eta}
ight) \left(rac{1+g}{1+r^f}
ight) \left(rac{\Pi^*}{\Pi}
ight)^{\phi_{\pi}-1} D.$$

A different *AD* is derived from the equations above, when the central bank hits the ZLB (1 + i = 1):

$$Y_{AD}^{ZLB} = D + \left(\frac{1+\beta}{\beta}\right)(1+g)\,\Pi D$$

The inflation rate at which the ZLB becomes binding is computed from the two arguments on the right-hand side of (3):

$$\Pi^{kink} = \left[\frac{1}{(1+r^f)}\right]^{\frac{1}{\phi_{\pi}}} \Pi^{*\frac{\phi_{\pi}-1}{\phi_{\pi}}}.$$

#### A.1.3 Proof of Proposition 1

Here we study the calibrations of the inflation target associated with the 5 panels in Figure 5. We start from the first and the last panel, which imply a unique equilibrium (a ZLB - U equilibrium in Panel A and a TR - FE equilibrium in Panel E). Then we derive the other cases. A proof of the Proposition 1 follows from the analysis of the case  $\Pi^* > \frac{1}{\delta(1+r^f)}$ . As explained in the main text, there are three possible steady state equilibria in the EMR OLG model (see Figure 3):

(A) ZLB - U that occurs at the intersection of the  $AD^{ZLB}$  and the  $AS^{DNWR}$ , and it features

$$Y = D + \left(\frac{1+\beta}{\beta}\right)(1+g)\,\delta\Pi^*D \le Y^f$$
$$i = 0$$

$$\Pi = \delta \Pi^* < \Pi^*;$$

(B) ZLB - FE that occurs at the intersection of the  $AD^{ZLB}$  and the  $AS^{FE}$ , and it features

$$Y = Y^f$$
  
 $i = 0$   
 $\Pi = \frac{1}{1 + r^f} \le \Pi^*;$ 

(C) TR - FE that occurs at the intersection of the  $AD^{TR}$  and the  $AS^{FE}$ , and it features

$$Y = Y^f$$
$$i > 0$$
$$\Pi = \Pi^*.$$

**Panel A.**  $\Pi^* < \frac{1}{1+r^f}$ . The second term in the max operator of equation (3) is lower than 1 for  $\Pi = \Pi^*$ , so i = 0 and a TR - FE equilibrium is impossible. As the resulting inflation level is  $\Pi < \Pi^* < \frac{1}{1+r^f}$  because of the ZLB, even a ZLB - FE equilibrium cannot exist and the only possible equilibrium is of the type ZLB - U.

**Panel E.**  $\Pi^* > \frac{1}{\delta(1+r^f)}$ . Even if the inflation level reaches its lower bound  $\Pi = \delta \Pi^*$ ,  $r = r^f$  (and so  $Y = Y^f$ ) can be achieved without hitting the ZLB. This can be verified by substituting *r* for  $r^f$  and  $\Pi$  for  $\delta \Pi^*$  in the Fisher equation (A15). As the ZLB is not binding (*i* > 0), *ZLB* – *U* and *ZLB* – *FE* equilibria cannot emerge and the unique equilibrium is of the type TR - FE.

**Panel B.**  $\Pi^* = \frac{1}{1+r^f}$ . There exists an equilibrium with inflation at the target and output at the potential in this case. In fact, the term  $(1+r^f)\Pi^*(\frac{\Pi}{\Pi^*})^{\phi_{\pi}}$  in equation (3) is 1 for  $\Pi = \Pi^*$ . This equilibrium features accordingly  $Y = Y^f$  (because  $r = r^f$ ), i = 0 and  $\Pi = \Pi^* = \frac{1}{1+r^f}$ , so it is a combination between ZLB - FE and TR - FE equilibria. Anyway, this is not the unique equilibrium, but there still exists a ZLB - U equilibrium because  $\Pi^* < \frac{1}{\delta(1+r^f)}$ .

**Panel C.**  $\frac{1}{1+r^f} < \Pi^* < \frac{1}{\delta(1+r^f)}$ . Given  $\frac{1}{1+r^f} < \Pi^*$ , the second term in the max operator of the Taylor rule (3) is greater than 1 for  $\Pi = \Pi^*$ , so the ZLB is not binding in correspondence of the inflation target and the natural interest rate. As a consequence, a TR - FE equilibrium exists, but it is not the unique equilibrium

given that  $\Pi^* < \frac{1}{\delta(1+r^f)}$ . Even ZLB - FE and ZLB - U equilibria emerge and, in particular, the ZLB - FE equilibrium differs from the type TR - FE ( $\frac{1}{1+r^f} = \Pi < \Pi^*$ ).

**Panel D.**  $\frac{1}{1+r^f} < \Pi^* = \frac{1}{\delta(1+r^f)}$ . For  $\Pi = \delta \Pi^*$  and  $r^f = r$ , the Fisher equation (A15) implies binding ZLB (i = 0). So, even if the DNWR is at work, for a zero nominal interest rate is possible to achieve  $Y = Y^f$ . This means that, along with a TR - FE equilibrium (which still exists because  $\Pi^* > \frac{1}{1+r^f}$ ), an equilibrium with binding ZLB survives. Given i = 0, it follows from the Fisher equation

$$\Pi = \delta \Pi^* = \frac{1}{1+r^f}.$$

Therefore this equilibrium is a combination between ZLB - U and ZLB - FE equilibria.

### A.2 Downward Nominal Wage Rigidity à la EMR

#### A.2.1 Steady State Equilibrium

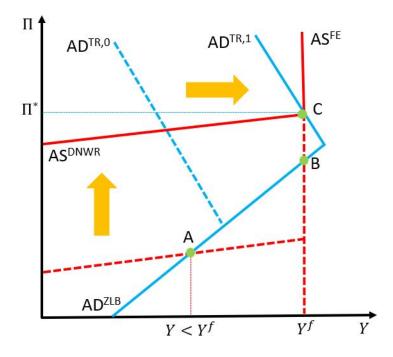
We assume a different specification of the DNWR:

$$W_t^* = \gamma \Pi^* W_{t-1} + (1 - \gamma) \, \alpha P_t \bar{L}^{\alpha - 1} \tag{A16}$$

The model is the same outlined in Appendix A.1, apart from this assumption which alters aggregate supply. For  $\Pi \ge \Pi^*$ , AS is still given by  $Y_{AS}^{FE} = Y^f$ , while it becomes

$$Y_{AS}^{DNWR} = \left[\frac{1 - \gamma \frac{\Pi^*}{\Pi}}{1 - \gamma}\right]^{\frac{\alpha}{1 - \alpha}} Y^f$$
(A17)

for  $\Pi < \Pi^*$ . This equation is derived from (A11), (A13) and (A16). It is represented by an upward sloping curve in Figure 8. If inflation falls below the target, wages cannot adjust to clear the labor market because of DNWR (A16), and involuntary unemployment determines a level of output lower than the potential one. This results in a positive relation between steady state inflation and output which is a direct consequence of a too high real wage: as inflation increases, the real wage approaches the level consistent with full employment, reducing the output gap. Although the segment of the AS corresponding to binding DNWR is not longer flat like in Section 2, the central mechanism behind our result still holds (Figure 8). Even if the DNWR depends on the "flexible" nominal wage,  $\alpha P_t \bar{L}^{\alpha-1}$ , the AS Figure 8: Raising the inflation target with our DNWR á la EMR



curve moves with the inflation target and so raising  $\Pi^*$  shifts the  $AS^{DNWR}$  upward. We can accordingly establish a proposition similar to Proposition 1 in Section 2 and Proposition 2 continues to hold.

**Proposition 5.** Assume  $r^f < 0$  and  $\gamma < 1$ . Then, if  $\Pi^* > \frac{1}{1+r^f}$ , there exists a unique, locally determinate, TR - FE equilibrium, where the ZLB is not binding, the inflation rate is equal to the target and output is at full employment, i.e., i > 0,  $\Pi = \Pi^*$ ,  $Y = Y^f$ .

### **Proof**:

There are three possible steady state equilibria in the EMR OLG model with DNWR (A16):

(A) ZLB - U that occurs at the intersection of the  $AD^{ZLB}$  and the  $AS^{DNWR}$ , and it features

$$Y = \left[\frac{1 - \gamma \frac{\Pi^*}{\Pi}}{1 - \gamma}\right]^{\frac{\omega}{1 - \alpha}} Y^f < Y^f$$

$$i = 0$$
$$\Pi = \frac{1}{1+r} < \Pi^*$$

(B) ZLB - FE that is identical to the equilibrium in the proof of Proposition 1;

(C) TR - FE that is identical to the equilibrium in the proof of Proposition 1.

If  $r^f < 0$ , three different cases can emerge and they are all depicted in Figure 9. *AD* can intersect *AS* on its upward sloping segment  $AS^{DNWR}$  and the resulting unique equilibrium is a ZLB - U (Panel A); *AD* can intersect *AS* on its vertical segment  $AS^{FE}$  and the unique equilibrium is a combination between a ZLB - FE and a TR - FE equilibrium, because  $Y = Y^f$ ,  $\Pi = \Pi^* = \frac{1}{1+r^f}$  and i = 0 (Panel B); *AD* can intersect *AS* on its vertical segment  $AS^{FE}$  and the only equilibrium is a TR - FE (Panel C). Now, we study the parameterizations of  $\Pi^*$  corresponding to these three cases. A proof of Proposition 5 follows from the analysis of the case  $\Pi^* > \frac{1}{1+r^f}$ .

**Panel A.**  $\Pi^* < \frac{1}{1+r^f}$ . The proof is the same of Proposition 1.

**Panel B.**  $\Pi^* = \frac{1}{1+r^f}$ . The second term in the max operator of equation (3) is 1 (binding ZLB) in correspondence of an inflation level equal to the target  $\Pi^*$ . So, the unique equilibrium is a combination between a ZLB - FE and a TR - FE equilibrium, given that  $Y = Y^f$  (in fact,  $r = r^f$ ), i = 0 and  $\Pi = \Pi^* = \frac{1}{1+r^f}$ .

**Panel C.**  $\Pi^* > \frac{1}{1+r^f}$ . The ZLB is never binding in this case, because the term  $(1+r^f)\Pi^*(\frac{\Pi}{\Pi^*})^{\phi_{\pi}}$  in the monetary policy rule (3) is greater than 1 for  $\Pi = \Pi^*$ . Therefore, the only possible equilibrium is a TR - FE.

### A.3 Appendix to SGU

#### A.3.1 Model

Unless otherwise mentioned, the notation is identical to that of the model in Appendix A.1.1. The representative household seeks to maximize the utility function

$$E_0 \sum_{t=0}^{\infty} \beta^t \left( \frac{C_t^{1-\sigma} - 1}{1-\sigma} \right)$$

where  $\sigma > 0$ , subject to the constraints

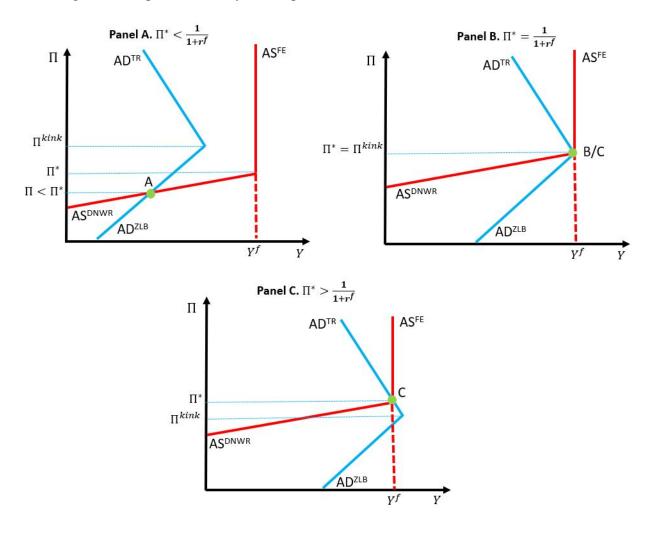


Figure 9: All possible steady state equilibria with our DNWR á la EMR

$$P_t C_t + B_t = W_t L_t + Z_t + (1 + i_{t-1}) B_{t-1}$$
$$lim_{j \to \infty} E_t \left[ \prod_{s=0}^j (1 + i_{t+s})^{-1} \right] B_{t+j+1} \ge 0.$$

 $C_t$  denotes the real consumption expenditure, while  $B_t$  is the value of risk-free bonds in nominal terms. The optimality conditions for the household's problem is the Euler equation

$$C_t^{-\sigma} = \beta (1+i_t) E_t \left[ \frac{C_{t+1}^{-\sigma}}{\Pi_{t+1}} \right]$$
(A18)

and the no-Ponzi-game constraint

$$\lim_{j \to \infty} E_t \left[ \prod_{s=0}^{j} (1+i_{t+s})^{-1} \right] B_{t+j+1} = 0$$

which holds with equality. The problem of the representative firm is the same illustrated in Appendix A.1.1, while the DNWR described in the main text is

$$\frac{W_t}{W_{t-1}} \ge \gamma_0 \left(\frac{L}{\bar{L}}\right)^{\gamma_1}.$$
(A19)

The aggregate resource constraint imposes

$$Y_t = C_t \tag{A20}$$

and the aggregate rate of unemployment is:

$$u_t = \frac{\bar{L} - L_t}{\bar{L}} \tag{A21}$$

#### A.3.2 Steady State Equilibrium

A competitive equilibrium is a set of processes  $\{Y_t, C_t, L_t, u_t, \Pi_t, W_t, i_t\}$  that solve (9), (11), (A11), (A13), (A18), (A19), (A20) and (A21), given the initial value for  $W_{-1}$ . We study the steady state equilibrium by analyzing aggregate demand and supply, which are characterized by two regimes. For  $\Pi \ge \gamma_0 = \Pi^*$ , *AS* is obtained from (9), (A11) and (A19):

$$Y_{AS}^{FE} = \bar{L}^{\alpha} = Y^f.$$

By combining the same equations, AS becomes

$$Y_{AS}^{DNWR} = \left[ \left( \frac{\Pi}{\gamma_0} \right)^{\frac{1}{\gamma_1}} \bar{L} \right]^{\alpha}$$

when  $\Pi < \gamma_0 = \Pi^*$ . Now, we turn to aggregate demand. For a positive nominal interest rate,

$$1+i=\frac{\Pi^*}{\beta}+\alpha_{\pi}\left(\Pi-\Pi^*\right)+\alpha_{y}\ln\left(\frac{Y}{Y^f}\right)$$

and *AD* can be computed from the Taylor rule by substituting 1 + i for its steady state value  $\frac{\Pi}{\beta}$ :

$$\ln Y_{AD}^{TR} = \ln Y^f - \frac{\beta \alpha_{\pi} - 1}{\beta \alpha_y} \left( \Pi - \Pi^* \right).$$

It can be alternatively expressed as:

$$Y_{AD}^{TR} = rac{Y^f}{e^{\Phi(\Pi - \Pi^*)}}$$

where  $\Phi = \frac{(\beta \alpha_{\pi} - 1)}{\beta \alpha_{y}}$ . If the ZLB binds (1 + *i* = 1), *AD* turns

$$\Pi = \beta$$

and it is computed by following the same steps as above.